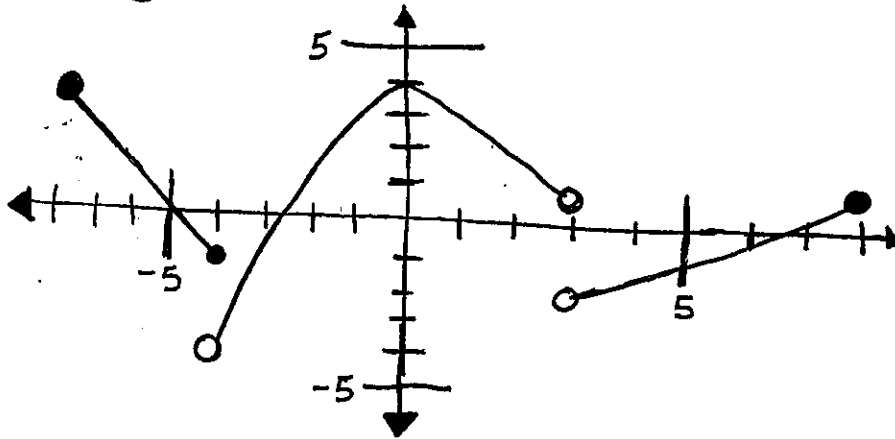


① Use the graph of $y=f(x)$ to answer the following questions.

$y=f(x)$



a) State the domain of $y=f(x)$

b) State the interval over which $y=f(x)$ is continuous

c) $f(-4)$

d) $f(0) =$

e) $f(3) =$

②
$$f(x) = \begin{cases} 3x+2 & x < 0 \\ (x-1)^2 & 0 \leq x < 5 \\ x-2 & x > 5 \end{cases}$$

Determine

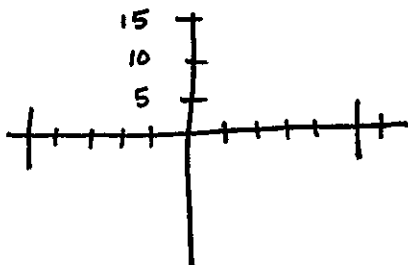
b) $f(0) =$

c) $f(5) =$

d) $f(4) =$

e) $f(10) =$

a) Draw $f(x)$



f) Is $f(x)$ continuous at $x=0$. Give reason why $f(x)$ is/is not continuous at $x=0$

③ Determine the limit of each:

$$a) \lim_{x \rightarrow 3} \frac{x^2 - 9}{x - 3}$$

$$f) \lim_{x \rightarrow 5} \frac{x^2 - 11x + 30}{x^2 - 25}$$

$$b) \lim_{x \rightarrow \infty} \frac{5x^2 + 2x - 3x^5}{x - 2}$$

$$g) \lim_{x \rightarrow \infty} \frac{\cos x}{x}$$

$$c) \lim_{x \rightarrow \infty} \frac{4x^3 + 5x - 2}{3 - 2x - 5x^4}$$

$$h) \lim_{x \rightarrow 0} \frac{2x + \sin 2x}{2x}$$

$$d) \lim_{x \rightarrow -\infty} \frac{5x^3 - 4x + 1}{4 - x^2}$$

$$i) \lim_{x \rightarrow \infty} \cos\left(\frac{1}{x}\right)$$

$$e) \lim_{x \rightarrow 0^-} \frac{x}{|x|}$$

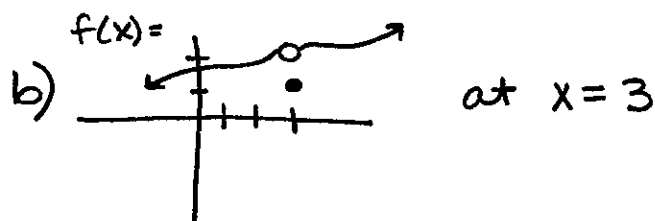
$$j) \lim_{x \rightarrow \infty} \frac{4x^3 - 3x + 2}{3x^3 + x^2 + x}$$

④ Determine if the function is continuous at the given x value. Show why the function is/is not continuous at the x value.

a) $f(x) = \frac{x^2 - 11x + 30}{x^2 - 25}$ at $x = 5$

circle one
 Continuous / ^{not} Continuous

Explain:



Continuous / ^{not} Continuous

Explain:

⑤ Given that $f(x)$ and $g(x)$ are defined for all x values and

$$\lim_{x \rightarrow c} f(x) = 6 \quad \lim_{x \rightarrow c} g(x) = 8$$

What is the $\lim_{x \rightarrow c} \frac{3f(x) + g(x)}{f(x)}$

⑥ Find the value of "a" so the function $g(x)$ is continuous:

$$g(x) = \begin{cases} 4x - 11 & x < 3 \\ ax^2 & x \geq 3 \end{cases}$$

⑦ The right end behavior model of the function $f(x) = 2x + e^{-x}$ is:

⑧ The left end behavior model of the function $f(x) = 2x + e^{-x}$ is:

⑨ Let $g(x) = x^2 - 3x + 4$

a) Find the average rate of change of g
over the interval $[1, 4]$

b) Find the rate of change of g at $x=3$

c) Find the equation of the line tangent
to g at $x=3$

d) Find the equation of the line normal
to g at $x=3$

⑩ Draw a function that meets the following conditions:

$$f(2) = 3$$

$$\lim_{x \rightarrow 5^+} f(x) = \infty$$

$$\lim_{x \rightarrow \infty} f(x) = \infty$$

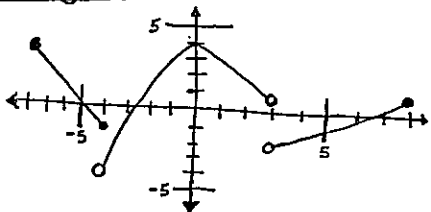
$$\lim_{x \rightarrow 2} f(x) = -1$$

$$\lim_{x \rightarrow 5^-} f(x) = -\infty$$

$$\lim_{x \rightarrow -\infty} f(x) = 1$$

① Use the graph of $y=f(x)$ to answer the following questions.

$y=f(x)$



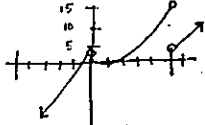
- a) State the domain of $y=f(x)$
 $[-8, 3) \cup (3, 8]$
- b) State the interval over which $y=f(x)$ is continuous $[-8, -4) \cup (-4, 3) \cup (3, 8]$
- c) $f(-4) = -1$ d) $f(0) = 4$ e) $f(3) = \text{d.n.e.}$

② $f(x) = \begin{cases} 3x+2 & x < 0 \\ (x-1)^2 & 0 \leq x < 5 \\ x-2 & x > 5 \end{cases}$

Determine

- b) $f(0) = 1$
 c) $f(5) = \text{d.n.e.}$
 d) $f(4) = 9$
 e) $f(10) = 8$

a) Draw $f(x)$.

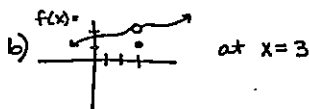


f) Is $f(x)$ continuous at $x=0$.
 Give reason why $f(x)$ is/is not continuous at $x=0$.
 Not, $\lim_{x \rightarrow 0} f(x) \neq f(0)$.

④ Determine if the function is continuous at the given x value. Show why the function is/is not continuous at the x value.

a) $f(x) = \frac{x^2 - 11x + 30}{x^2 - 25}$ at $x=5$ Circle one: Continuous / ~~not continuous~~

Explain: because when $x=5$ the denominator is zero



Continuous / ~~not continuous~~

Explain: because $\lim_{x \rightarrow 3} f(x) \neq f(3)$

⑤ Given that $f(x)$ and $g(x)$ are defined for all x values and

$\lim_{x \rightarrow c} f(x) = 6$ $\lim_{x \rightarrow c} g(x) = 8$

What is the $\lim_{x \rightarrow c} \frac{3f(x) + g(x)}{f(x)}$ $\frac{3(6) + 8}{6} = \frac{26}{6} = \frac{13}{3}$

③ Determine the limit of each:

a) $\lim_{x \rightarrow 3} \frac{x^2 - 9}{x - 3} = \lim_{x \rightarrow 3} \frac{(x+3)(x-3)}{x-3} = \lim_{x \rightarrow 3} (x+3) = 6$

f) $\lim_{x \rightarrow 5} \frac{(x-6)(x-5)}{x^2 - 11x + 30} = \lim_{x \rightarrow 5} \frac{(x-6)(x-5)}{(x-5)(x-6)} = \lim_{x \rightarrow 5} \frac{x-6}{x-6} = \frac{1}{10}$

b) $\lim_{x \rightarrow \infty} \frac{5x^2 + 2x - 3x^5}{x^2 - 2} = -\infty$
 EB Model: $y = -3x^1$

g) $\lim_{x \rightarrow \infty} \frac{\cos x}{x} = 0$

c) $\lim_{x \rightarrow \infty} \frac{4x^3 + 5x - 2}{3 - 2x^2 - 5x^4} = 0$
 EB Model: $y = -\frac{4}{5}x$

h) $\lim_{x \rightarrow 0} \frac{2x + \sin 2x}{2x} = 2$
 $\lim_{x \rightarrow 0} \frac{2x}{2x} + \frac{\sin 2x}{2x} = 1 + 1 = 2$

d) $\lim_{x \rightarrow -\infty} \frac{5x^3 - 4x + 1}{4 - x^2} = \infty$
 EB Model: $y = -5x$

i) $\lim_{x \rightarrow \infty} \cos\left(\frac{1}{x}\right) = 1$

e) $\lim_{x \rightarrow 0^-} \frac{x}{|x|} = -1$

j) $\lim_{x \rightarrow \infty} \frac{4x^3 - 3x + 2}{3x^3 + x^2 + x} = \frac{4}{3}$
 EB Model: $y = \frac{4}{3}$

⑥ Find the value of 'a' so the function $g(x)$ is continuous:

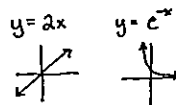
$g(x) = \begin{cases} 4x - 11 & x < 3 \\ ax^2 & x \geq 3 \end{cases}$

$4x - 11 = ax^2$
 $4(3) - 11 = a(3)^2$

$1 = 9a$
 $\frac{1}{9} = a$

⑦ The right end behavior model

of the function $f(x) = 2x + \frac{e^{-x}}{0}$ is:



$f(x) = 2x$ is the right hand behavior model

⑧ The left end behavior model

of the function $f(x) = 2x + e^{-x}$ is:

e^{-x} is going up faster than $2x$ is going down so left hand behavior model

Be sure you can explain your reason for choosing your answer

$f(x) = e^{-x}$

9) Let $g(x) = x^2 - 3x + 4$

a) Find the average rate of change of g over the interval $[1, 4]$

$$\begin{aligned} \text{ave. rate of change} &= \frac{g(4) - g(1)}{4 - 1} = \frac{[8] - [2]}{3} \\ &= \frac{[(4)^2 - 3(4) + 4] - [(1)^2 - 3(1) + 4]}{4 - 1} = \boxed{2} \end{aligned}$$

b) Find the rate of change of g at $x=3$

$$\begin{aligned} \lim_{h \rightarrow 0} \frac{g(3+h) - g(3)}{(3+h) - (3)} &= \lim_{h \rightarrow 0} \frac{3h + h^2}{h} \\ &= \lim_{h \rightarrow 0} 3 + h \\ &= \boxed{3} \end{aligned}$$

$$\begin{aligned} \lim_{h \rightarrow 0} \frac{[(3+h)^2 - 3(3+h) + 4] - [(3)^2 - 3(3) + 4]}{h} &= \lim_{h \rightarrow 0} \frac{[9 + 6h + h^2 - 9 - 3h + 4] - [4]}{h} \\ \lim_{h \rightarrow 0} \frac{[9 + 6h + h^2 - 9 - 3h + 4] - [4]}{h} & \end{aligned}$$

c) Find the equation of the line tangent to g at $x=3$

$$\begin{aligned} g(3) &= (3)^2 - 3(3) + 4 \\ &= 4 \\ (3, 4) \end{aligned}$$

$m = 3$ is 3 from part b)

$$\boxed{y - 4 = 3(x - 3)}$$

d) Find the equation of the line normal to g at $x=3$

$$\boxed{y - 4 = -\frac{1}{3}(x - 3)}$$

10) Draw a function that meets the following conditions:

$$f(2) = 3$$

$$\lim_{x \rightarrow 5^+} f(x) = \infty$$

$$\lim_{x \rightarrow \infty} f(x) = \infty$$

$$\lim_{x \rightarrow 2} f(x) = -1$$

$$\lim_{x \rightarrow 5^-} f(x) = -\infty$$

$$\lim_{x \rightarrow -\infty} f(x) = 1$$

