

Continuity

Section 2.3

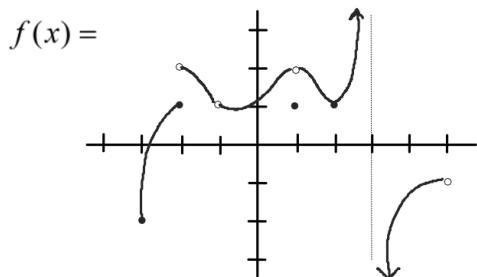
Continuity at a point:

$f(x)$ is continuous at $x = c$ iff

1) $f(c)$ exists

2) $\lim_{x \rightarrow c} f(x)$ exists

3) $f(c) = \lim_{x \rightarrow c} f(x)$



Domain: $[-3, -1) \cup (-1, 3) \cup (3, 5)$

Points of Discontinuity:

$x = -2, -1, 1, 3, 5$

Why are they points of discontinuity?

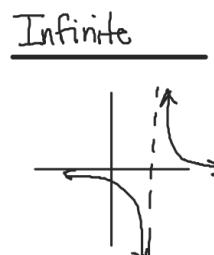
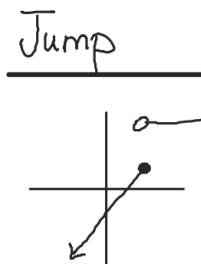
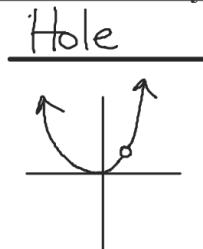
$x = -2$ $\lim_{x \rightarrow -2} f(x)$ d.n.e.	$x = 3$ $f(3)$ d.n.e.
$x = -1$ $f(-1)$ d.n.e.	$x = 5$ $f(5)$ d.n.e.
$x = 1$ $f(1) \neq \lim_{x \rightarrow 1} f(x)$	

Domain of a Function

Non-continuous points
Continuous points

where you find
the derivative of a function

Types of Discontinuity



Name the type of discontinuity within each function

1. $f(x) = \frac{1}{x+3}$

infinite

2. $f(x) = \frac{(x+2)(x-3)}{x-3}$

$= x+2$

hole

3. $f(x) = \begin{cases} 2 & x < -1 \\ 3 & x > -1 \end{cases}$

jump

Continuity of a function

Determine where the function is continuous and discontinuous.

4. $f(x) = \frac{x+2}{x+1}$

discont $\Rightarrow x = -1$
infinite

continuous: $(-\infty, -1) \cup (-1, \infty)$

5. $f(x) = \sqrt{x-2}$

cont: $[2, \infty)$

6. $f(x) = \sqrt{5-3x}$

$$5-3x \geq 0$$

$$-3x \geq -5$$

$$x \leq \frac{5}{3}$$

cont. on $(-\infty, \frac{5}{3}]$

7. $f(x) = x^2 + 5$

cont. $(-\infty, \infty)$

8. $f(x) = \ln(1-x)$

discont. $\Rightarrow x = 1$

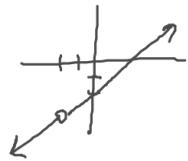
infinite discon.

cont. on $(-\infty, 1)$

For problems with removable discontinuity (#25-29)

Give the formula for the extended function that is continuous at the indicated point.

9. $f(x) = \frac{x^2-4}{x+2}$



Plan A

$$f(x) = \frac{(x+2)(x-2)}{x+2}$$

$$\tilde{f}(x) = x-2$$

Plan B

$$f(x) = \begin{cases} \frac{x^2-4}{x+2} & \text{when } x \neq -2 \\ -4 & \text{when } x = -2 \end{cases}$$