

## Warm-Up After MVT

Determine if the MVT applies to the given interval if not, explain why if so, find the value of  $x$  that satisfies the MVT without a calculator.

1.  $f(x) = |x - 1|$  on  $[-3, 5]$

2.  $f(x) = |x - 1|$  on  $[-3, 1]$

3.  $f(x) = x^2$  on  $(0, 2]$

4.  $f(x) = \ln(x + 3)$  on  $[-2, 2]$

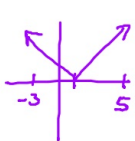
5.  $f(x) = x^{\frac{2}{3}}$  on  $[-2, 2]$

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1.  $f(x) = |x - 1|$  on  $[-3, 5]$

$$f'(x) = \begin{cases} -1 & x < 1 \\ 1 & x > 1 \end{cases}$$



MVT does not apply  
b/c  $f(x)$  is not diff.  
at  $x = 1$

2.  $f(x) = |x - 1|$  on  $[-3, 1]$

$$\frac{|1 - 1| - |-3 - 1|}{1 - (-3)} = -1$$

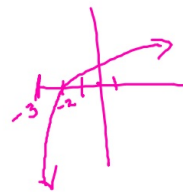
$$\frac{-4}{4} = -1 \quad \text{all } x \text{ values on the interval } [-3, 1]$$

$$-1 = -1$$

3.  $f(x) = x^2$  on  $(0, 2]$

MVT d.n. apply on  
an open interval

4.  $f(x) = \ln(x + 3)$  on  $[-2, 2]$



$$\frac{\ln(2+3) - \ln(-2+3)}{2 - (-2)} = \frac{1}{x+3}$$

$$\frac{\ln(5)}{4} = \frac{1}{x+3}$$

$$x+3 = \frac{4}{\ln(5)}$$

$$x = \frac{4}{\ln(5)} - 3$$

5.  $f(x) = x^{\frac{2}{3}}$  on  $[-2, 2]$

$$f'(x) = \frac{2}{3} x^{-\frac{1}{3}} = \frac{2}{3x^{\frac{1}{3}}}$$

MVT d.n. apply  $f$  is not diff.  
at  $x = 0$ .